地球内部磁気圏統合データ同化システム開発の現状

Energetic neutral atom

(ENA)

Cold ions

(Plasmasphere)

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Motivation

In our past studies...

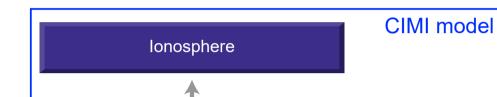
- The temporal evolution of the ring current was reproduced by data assimilation of the IMAGE/HENA data into a ring current model (Nakano et al., 2008).
- The temporal evolution of the plasmasphere was reproduced by data assimilation of the IMAGE/EUV data into a plasmasphere model (Nakano et al., 2014).

Our two data assimilation methods were based on similar frameworks. Thus, these two methods can be combined.

The plasmasphere is located deep inside of the magnetosphere, and the ring current is typically distributed just outside the plasmasphere.

In terms of estimating the electric field distribution, the ENA emission from the ring current would provide complementary information to the EUV emission from the plasmasphere.

Model and method

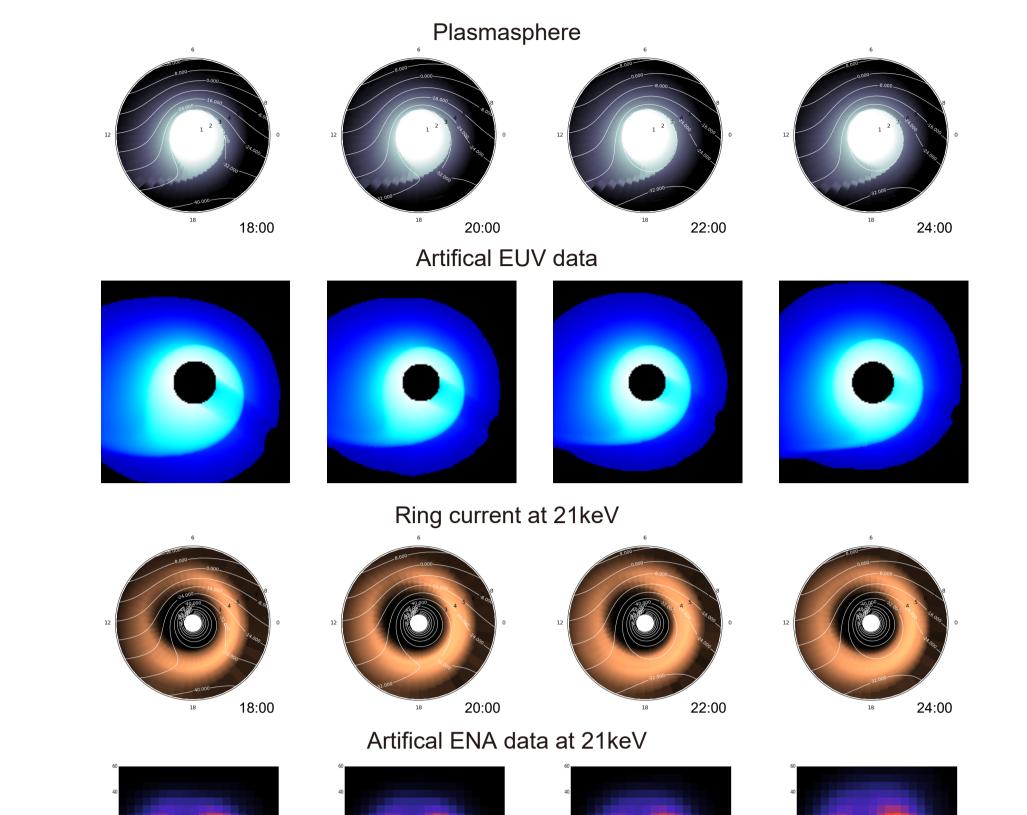


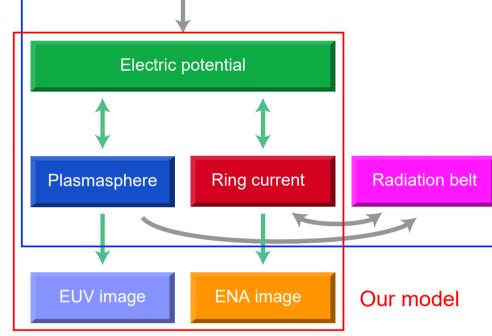
We use an inner magnetosphere model in which the plasmasphere and the ring current are driven by a common magnetic and electric fields.

High energy ions

(Ring current)







This model is based on the Comprehensive Inner Magnetosphere Ionosphere (CIMI) model (Fok et al., 2014), but the magnetosphere-ionosphere coupling and the plasma-wave effects on the radiation belt are turned off.

At presenet, the IMAGE/HENA data at two channels (20-27keV and 39-50keV) and the IMAGE/EUV data are considered for our data asimilation.

The evolution of the ring current is computed using a four dimensional model based on the Boltzmann equation (Fok et al., 1997):

$$\frac{\partial \overline{f}}{\partial t} + \langle \dot{\lambda}_{i} \rangle \frac{\partial \overline{f}}{\partial \lambda_{i}} + \langle \dot{\phi}_{i} \rangle \frac{\partial \overline{f}}{\partial \phi_{i}} = -v\sigma \langle n \rangle \overline{f} - \left(\frac{\overline{f}}{0.5\tau_{b}}\right)_{\text{losscone}},$$

where $\langle \dot{\lambda}_i \rangle$ and $\langle \dot{\phi}_i \rangle$ indicate the bounce-averaged velocity which depends on the background magnetic and electric fields.

The evolution of the plasmaspheric plasma density \overline{N} can be described by the following equations (Ober et al., 1997):

 $\frac{\partial \overline{N}}{\partial t} - \frac{\nabla \Phi \times \boldsymbol{B}}{B^2} \cdot \frac{\partial \overline{N}}{\partial \boldsymbol{x}} = 0. \qquad \begin{array}{c} \Phi : & \text{Electric potential,} \\ \boldsymbol{B} : & \text{Magnetic field.} \end{array}$

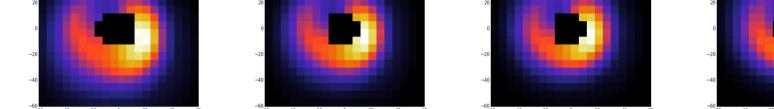
The electric potential distribution is treated as an unknown factor to be estimated. Here we represent the electric potential distribution by the sum of the Volland-Stern type potential and the series of cylindrical functions as

$$\Phi = \Phi_0 \left[\left(\frac{r}{R}\right)^2 \sin \phi + \sum_{n,j} a_{n,j} \mathcal{J}_n \left(\xi_{nj} \frac{r}{R}\right) \cos n\phi + \sum_{n,j} b_{nj} \mathcal{J}_n \left(\xi_{nj} \frac{r}{R}\right) \sin n\phi \right]$$

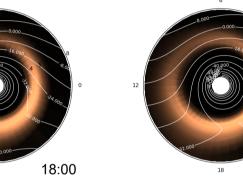
where *R* is the equatorial radius of the outer boundary of the simulation domain, \mathcal{J}_n is the *n*-th order Bessel function, and ξ_{nj} is the positive roots of $\mathcal{J}_n(\xi_{nj}) = 0$.

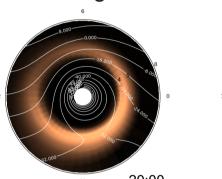
The parameters Φ and the coefficients a_{ni} and b_{ni} are to be estimated using the data assimilation.

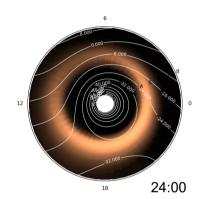
The ensemble transform Kalman filter (Bishop et al., 2001) was used in order to achieve the estimation of the plasmasphere, ring current, and electric field. (Assimilation cycle: 30 minutes; ensemble size: 64; covariance inflation factor: 1.05 for every 30 min.)



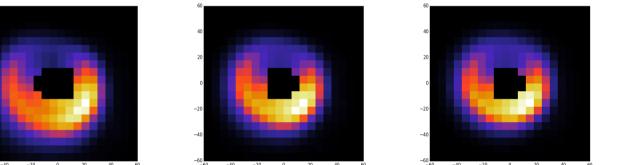


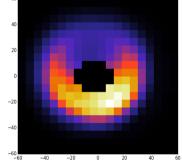




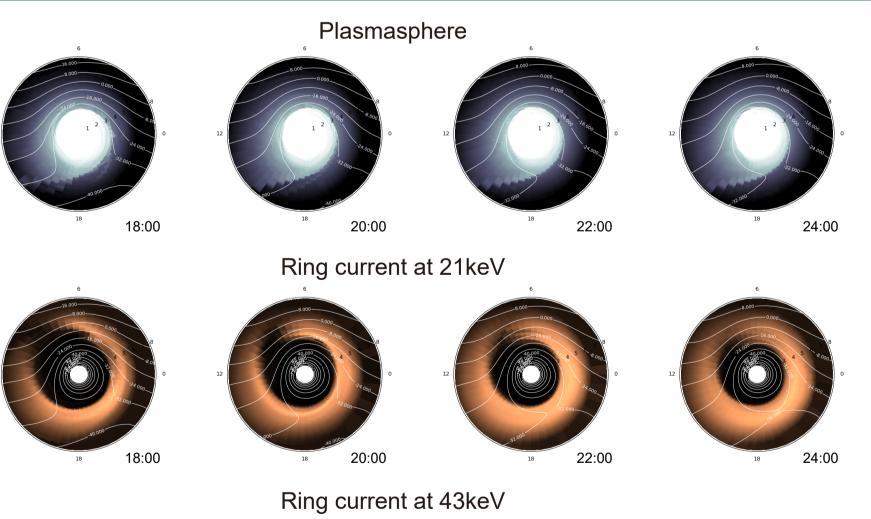


Artifical ENA data at 43keV

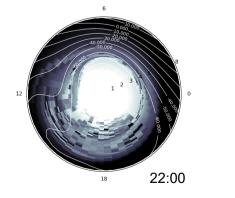


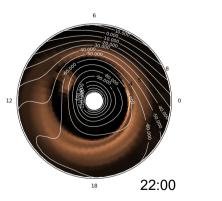


Result of the experiment with the artificial data

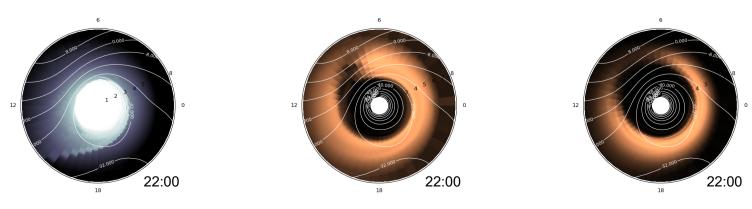


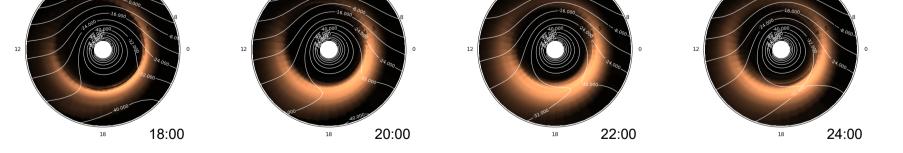
Only with the HENA data





Only with the EUV data





Future tasks:

At present, the spatial pattern of the electric potential is assumed to be constant over time. But, this should be resolved.

It is also necessary to implement the estimation of the initial state of the plasmasphere.

References

Bishop et al. (2001): Adaptive sampling with the ensemble transform Kalman filter. Part I: Theoretical aspects, Mon. Wea. Rev., v. 129, p. 420.
Fok et al. (2001): Comprehensive computational model of Earth's ring current, J. Geophys. Res., v. 104, p. 14,557, doi:10.1029/2000JA000235.
Fok et al. (2014): The Comprehensive Inner Magnetosphere-Ionosphere Model, J. Geophys. Res., v. 119, p. 7,522, doi:10.1002/2014JA020239.
Nakano et al. (2008): A method for estimating the ring current structure and the electric potential distribution using ENA data assimilation, J. Geophys. Res., v. 113, doi:10.1029/2006JA011853.

Nakano et al. (2014): Estimation of temporal evolution of the helium plasmasphere based on a sequence of IMAGE/EUV images, J. Geophys. Res., v. 119, p. 3,708, doi:10.1002/2013JA019734.

Ober et al. (1997): Formation of density troughs embedded in the outer plasmasphere by subauroral ion drift events, J. Geophys. Res., v. 102, p. 14,595.



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